Assessing the risk of COVID-19 epidemic resurgence

in relation to the Delta variant and to vaccination passes

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Abstract

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The introduction of COVID-19 vaccination passes (VPs) by many countries coincides with the Delta variant fast becoming dominant across Europe. A thorough assessment of their impact on epidemic dynamics is still lacking. Here, we propose the VAP-SIRS model that considers possibly lower restrictions for the VP holders than for the rest of the population, imperfect vaccination effectiveness against infection, rates of (re-)vaccination and waning immunity, fraction of never-vaccinated, and the increased transmissibility of the Delta variant. Some predicted epidemic scenarios for realistic parameter values yield new COVID-19 infection waves within two years, and high daily case numbers in the endemic state, even without introducing VPs and granting more freedom to their holders. Still, suitable adaptive policies can avoid unfavorable outcomes. While VP holders could initially be allowed more freedom, the lack of full vaccine effectiveness and increased transmissibility will require accelerated (re-)vaccination, NOTE: This preprint reports new research that has not been certified by peer review and should not be used to guide clinical practice. wide-spread immunity surveillance, and/or minimal long-term common restrictions.

Introduction

In the past, governments have required proof of vaccination for travel, with yellow fever being the bestknown example, and the only disease for which a certificate is needed as a precondition of entry to a country in compliance to the International Health Regulations [1]. However, the idea that proof of vaccination will become a prerequisite for crossing borders or to enter facilities, visit businesses premises, participate in events, and generally enjoy more freedom, has only arisen in the context of combatting the COVID-19 epidemic. Despite technical challenges, scientific uncertainties, and ethical and legal dilemmas, the idea of VPs, i.e., documents issued on the basis of vaccination status, is now receiving unprecedented attention [2, 3, 4]. The Commission of the European Union (EU), in an effort to ensure a uniform pan-European approach, as similar initiatives for VPs were emerging at national level, put forth a proposal for a framework of issuing, verifying and accepting interoperable vaccination certificates to be implemented across the EU [4], along with a corresponding proposal for third-country nationals re-41 siding in the EU [5]. The proposal, in its amended form, for the 'Digital COVID Certificates' (DCCs), took effect on July 1, 2021. Many consider the EU DCCs, and other forms of VPs in general, as tools to restore people's freedoms and increase well-being, whilst allowing economies to reopen. Finally, even without VPs, vaccinations alone may result in less stringent behavior. Those vaccinated may feel more secure and restrict themselves less from contacts they would refrain from when not being vaccinated. 46 The introduction of VPs and consequent changes in behavior coincided with the emergence of new 47 variants of concern of the virus [6]. Notably, the Delta variant (B.1.617.2) was detected in many countries across Europe, causing a resurgence of COVID-19 in the United Kingdom at a startling pace [7, 8]. Delta has been estimated to be 50% more transmissible than the Alpha variant (B.1.1.7), already estimated to be 50% more transmissible than the parental strain [9, 10, 11]. 51 Evidence indicates vaccine effectiveness can greatly vary [12, 13] and it may be compromised due 52 to escape variants [14] and waning immunity [15, 16, 17, 18]. Preliminary data from several countries 53 indicate reduced vaccine effectiveness against the infection with the Delta variant compared to the Alpha variant [19, 20, 21], even as low as 64% for the Comirnaty (Pfizer-BioNTech) vaccine according to unpublished data from Israel [22]. Emerging evidence suggests that the vaccines are still highly effect at preventing serious illness and hospitalization [11, 20, 21]. 57 Still, avoiding another COVID-19 infection resurgence remains a valid and potentially attainable 58 goal [23]. An estimated 10% of COVID-19 infections will have long-term sequelae (long COVID), posing an increasing threat to national health systems [24, 25]. Finally, large numbers of infected create

a large pool of virus hosts, resulting in more replications of the virus and higher chances of emergence of mutations conferring evolutionary advantage, including increased transmissibility and antigenicity. 62 To detect the emerging variants, wide-spread surveillance of genetic and antigenic changes in the virus population has to be conducted, together with experiments elucidating their phenotypic implications [26]. Such needed comprehensive surveillance and experiments may become stalled for a large population of infected. Given these circumstances, it is critically important to understand the impact of key risk factors such as: vaccine ineffectiveness, slow vaccination rate, waning immunity, fraction of individuals 67 in the population who will never become vaccinated, and finally the levels of restrictions, on infection dynamics. Not being aware of the risks and their consequences, and a false sense of security, including when approaching higher vaccination coverage, may result in policymakers opting to select suboptimal levels of restrictions. Various models have been developed to inform vaccination strategies [27, 28, 29, 30, 31, 32, 33, 72 34, 35]. One such effort indicates lower vaccine effectiveness coupled with an increase in social contact among those vaccinated (behavioral compensation) may undermine vaccination effects, even without considering immunity waning [36, 37]. Scenarios for the post-vaccination era were also considered by 75 Sandmann and colleagues (2021), finding that under realistic scenarios periodic epidemics are likely [38]. 76 So far, there has been no model to focus on the medium- and long-term impact of relaxing restrictions 77 for VP holders, with due consideration to vaccine effectiveness, durability of response, and vaccine hesitancy, especially in the context of the increased transmissibility of the Delta variant. Given the implementation of the EU DCC, and emerging heterogeneous measures on utilising the VPs for different purposes at national level by establishing different levels of freedom for VP holders in terms of accessing premises, facilities, travelling within a country, etc., it is important to examine the broad parameters determining how to optimise the implementation of measures such as the EU DCC and other VPs. 83 To address these needs, we propose a mathematical VAP-SIRS model, which accounts for key parameters affecting current infection dynamics, such as for lower restrictions for VPs holders than for the rest of the population, imperfect vaccination effectiveness against infection, rates of (re-)vaccination and waning immunity, and the increased transmissibility of the Delta variant, which all impact the effective reproduction number of the virus. The model predicts the impact of restrictions for VP holders and the rest of the population on epidemic thresholds for various parameter settings, and delivers a systematic framework to assess key considerations for policymaking.

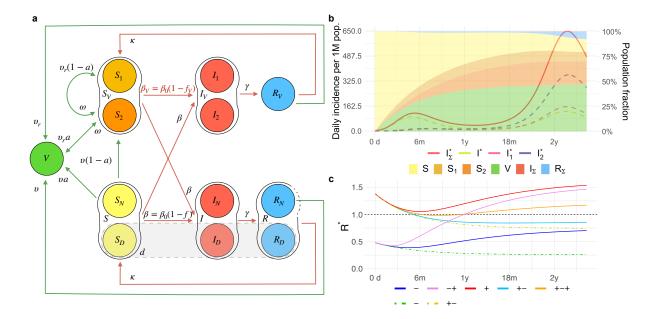


Figure 1: The VAP-SIRS model and its predicted scenarios. a. Graphical scheme of the VAP-SIRS model. b, c. Predicted scenarios for the reference setup for the Delta variant, with vaccine effectiveness a = 0.79 (corresponding to the effectiveness of the Comirnaty vaccine against infection with the Delta variant), slow (re-)vaccination rate ($v = v_r = 0.004$; typical for many European countries), slow immunity waning $\omega = 0.002$, low fraction of never-vaccinated (d = 0.12; corresponding to the fraction in the United Kingdom) and proportional mixing (see Methods). b. Color curves: Timeline of daily incidence per 1 million inhabitants in different infected compartments for the combination of restrictions f = 0.77and $f_{\rm v}=0.55$. A variable with the asterisk (*) indicates that we consider a daily incidence over the corresponding variable, and by I_{Σ}^* we mean the sum of all daily infected $(I_D^* + I_N^* + I_1^* + I_2^*)$. Color bands: Muller plot of the population structure (the width of the color band in the y axis) as a function of time (x axis) for the same parameter settings; by I_{Σ} and R_{Σ} we denote $I + I_{V}$ and $R + R_{V}$, respectively. c. Time evolution of the instantaneous reproduction number R^* (y axis) depending on the number of days counted from the start of the vaccination program (x axis), in five different scenarios describing the epidemic evolution: overcritical (+, red, f = 0.77 and $f_v = 0.38$), subcritical (-, blue, f = 0.92 and $f_{\rm v}=0.71$), initially and eventually overcritical (+-+, orange, the same restrictions as in **b**: f=0.77 and $f_{\rm v}=0.55$), eventually overcritical (-+, pink, f=0.92 and $f_{\rm v}=0.38$), and eventually subcritical (+-, cyan, with f = 0.77 and $f_v = 0.71$). As controls, two additional scenarios of the epidemic evolution are presented, corresponding to no implementation of VPs and no changes in behavior due to vaccination: subcritical (another example of - scenario, green) with $f = f_v = 0.92$ and eventually subcritical (another example of +- scenario, yellow) with $f = f_v = 0.77$, both plotted with dot-dashed line.

91 Results

The VAP-SIRS model of the impact of COVID-19 VPs

The VAP-SIRS model extends the classical SIRS model [39] (red arrows in Figure 1a) with additional states and parameters that describe the dynamics of vaccination rollout in a population (green arrows in Figure 1a). To this end, we consider the following subpopulations: (i) initially susceptible S_N , who, if successfully vaccinated, populate the immune group V, with rate av, where v is the vaccination rate

and a is the vaccination effectiveness, (ii) susceptible who were vaccinated but did not gain immunity (S_1) , (iii) vaccinated, whose immunity waned with rate ω and who became susceptible again (S_2) , (iv) susceptible, who are not and will never get vaccinated (S_D) . The S_D compartment contains people who for health reasons cannot receive current types of vaccines, as well as individuals who do not get 100 vaccinated because of hesitancy, beliefs or other individual reasons. The fraction of the population that 101 will never be vaccinated is denoted by d. Additionally, revaccination of S_2 populates V with rate av_r . 102 All recovered, unless in the recovered compartment R_D , are also subject to vaccination. Before the 103 recovered in the R_V lose immunity, they might be revaccinated, and, thus, populate the V group with 104 rate v_r (similarly, R_N are vaccinated with rate v). In this case, vaccination effectiveness is fixed to 105 1, which is substantiated on the basis of the fact that vaccination combined with a previous infection 106 should confer a much stronger protection than only vaccination of a susceptible individual. Across the 107 manuscript, we assume the revaccination and vaccination rates are equal, $v_r = v$. 108

The presented model analysis is performed for carefully selected parameter setups. We consider 109 two different vaccination rates a, 0.004 and 0.008 doses per person daily, chosen on the basis of the 110 current rates observed in Europe [40, 41]. As vaccine effectivenesses for the Delta variant, we consider 111 0.6 and 0.79, which were reported as the effectivenesses of the most widely used vaccines: Vaxzevria 112 (AstraZeneca) and Comirnaty (BioNTech/Pfizer) respectively for this variant [20]. For the Alpha 113 variant, the effectivenesses of the same vaccines for that variant are considered instead, namely 0.79 114 (Vaxzevria) and 0.92 (Cominarty) [20]. We consider realistic fractions d of never-vaccinated equal 115 to 0.12 (optimistic), and 0.3 (pessimistic), reported for the United Kingdom and France, respectively [https://ourworldindata.org/, as of June 15th, 2021]. Furthermore, two post-vaccination immunity wan-117 ing rates ω are considered corresponding to optimistic (500 days; $\omega = 1/500$) and pessimistic (200 days; 118 $\omega=1/200$) average immunity duration periods, reflecting emerging data on large individual variation 119 of immunity waning and other key factors influencing this process [15, 18, 42, 43, 44]. There remains 120 uncertainty regarding the waning time for natural immunity, and whether it varies between the different SARS-CoV-2 variants, but early evidence indicates it lasts at least 180 days [45, 46, 47]. Hence, we 122 consider an optimistic scenario of natural immunity lasting on average similarly long as the optimistic 123 immunity gained via vaccination: 500 days (corresponding to natural immunity waning rate $\kappa = 0.002$). 124 Based on the current studies, we fix the generation time to 6 days ($\gamma = 1/6$) [48, 49]. 125

We assume that VP holders are all those who completed at least one complete vaccination cycle, i.e., one dose or two doses depending on the vaccine used (Fig. 1), which is also the basis on which the EU DCC is issued. The restriction level (ranging from 0 to 1) is introduced as a modulator of the SARS-

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CoV-2 reproduction number. Here, we consider that without any restrictions, the basic reproduction 129 number for the B.1.617.2 variant (Delta) is equal to 6 (an optimistic estimate based on [50, 51]), while 130 for the B.1.1.7 variant (Alpha) an optimistic estimate is equal to 4 [48, 49]. Two levels of restrictions are 131 considered: restrictions f_v for contacts among VP holders, as well as restrictions f for contacts of the VP 132 holders with the rest of the population and for contacts within the rest of the population. The impact of 133 VPs is studied assuming that $f_v < f$: a VP holder has more freedom of contact with other VP holders, or 134 is generally subject to fewer restrictions on the VP holders than the rest of the population. Importantly, 135 in general f and f_v should be interpreted as the net effect of all combined factors that reduce the repro-136 duction number of the virus within the respective groups: all applied non-pharmaceutical interventions, 137 including testing and isolation, together with the resulting changes in behavior. The situation where no 138 VPs are implemented, hence the vaccinated have the same restrictions as the rest of the population, and 139 there are no changes of behavior due to vaccination, is modeled by fixing $f_v = f$. Finally, to analyze 140 the impact of social behavior, we consider two types of mixing between subpopulations: proportional 141 (typical for SIR models) and preferential, where the VP holders prefer contacts with other VP holders. 142 See Methods for a detailed model description.

VAP-SIRS predicts a possible infection resurgence despite vaccinations

VAP-SIRS predicts unfavourable epidemic dynamics for a wide range of parameters, both for the Delta 145 and the Alpha variants. As an example consider the Delta variant, and vaccine effectiveness a = 0.79 (the 146 effectiveness of the Comirnaty vaccine against the Delta variant), (re-)vaccination rates $v = v_r = 0.004$, 147 low never-vaccinated fraction d = 0.12 (reported for the United Kingdom), low immunity waning rate 148 $\omega = 0.002$, low natural immunity rate loss $\kappa = 0.002$, and proportional mixing. This set of parameters 149 corresponds to a seemingly safe setup, which we will call the reference setup. The impact of various 150 parameter changes with respect to this reference will be considered below. For such a setup, consider 151 medium-high restrictions level f = 0.77 for contacts of the VP holders with the rest of the population 152 and within the rest of the population, along with a restrictions reduction for the VP holders compared to 153 the rest of the population by around 30%, resulting in medium restrictions $f_v = 0.55$ for VP holders. 154 For these parameters, the model predicts a small wave of infections shortly after the vaccination program 155 starts, followed by a large wave later (color curves Fig. 1b). This behavior is explained by the population 156 structure (Muller plot, Fig. 1b) and can only happen due to the different levels of restrictions for the 157 VP holders and the rest of the population. In this scenario, the first wave is driven by the unvaccinated 158 susceptibles (S_N) and suppressed by ongoing vaccination, as expected. Interestingly, the second, larger 159

wave is driven by the S_V group. The S_V group is composed of the number of individuals for whom the vaccine was ineffective (S_1) and those vaccinated who lose their immunity and are not yet revaccinated (S_2) .

Stability analysis identifies potential scenarios for the COVID-19 epidemic depending on the restrictions imposed on VP holders and the rest of the population.

To assess the epidemic evolution in different scenarios, we analyse stability by linearising the model 165 equations with I = R = 0 and introduce the instantaneous reproduction number R^* (see Methods). 166 $R^*(t)$ is the reproduction number that would be observed at time t, given the restrictions $\mathbf{f} = (f, f_v)$ 167 and the composition of the population, where the number of infected is very small. For $R^*(t) > 1$, 168 switching to f at time t results in an overcritical epidemic evolution, with an initially exponential growth 169 of infections; for $R^*(t) < 1$, switching to **f** at time t results in a subcritical epidemic evolution, where 170 the number of active cases decreases to zero. The R^* is more informative of epidemic thresholds than 171 the standard effective reproduction number, as it does not depend on the actual number of infected and recovered. 173

Assuming the reference setup for the Delta variant, we consider five choices of restriction combina-174 tions (prototypical for five regions of the parameter space, see Figure 2), leading to different time profiles 175 of R^* (Fig. 1c). As control setups, we introduce two settings that represent policies in a given population 176 without the implementation of the VPs, one with a common high restriction level $f = f_v = 0.92$, which 177 keeps the epidemic subcritical (scenario denoted -, green dot-dashed line in Fig. 1c), and one with a 178 common medium-high restriction level $f = f_v = 0.77$, which results in a time evolution fo R^* from 179 overcritical to subcritical (denoted +-, yellow dot-dashed line in Fig. 1c). In such settings, in case VPs 180 are introduced, VP holders can gain low (<20%), medium (20-50%) or high (>50%) restriction reduction 181 with respect to the restrictions for the rest of the population. Granting high restriction reductions to VP 182 holders, both with mid-high and with high restrictions enforced for the rest of the population, eventually 183 leads to an overcritical epidemic (red and pink curve in Fig. 1c: the red curve shows a persistent overcrit-184 ical epidemic, a scenario denoted -, while the pink curve shows an epidemic that is initially subcritical 185 and then becomes overcritical, a scenario denoted -+). Medium restriction reductions for VP holders, 186 along with high restrictions for the rest of the population, yield a subcritical epidemic evolution (another 187 example of scenario -, blue curve in Fig. 1c). When mid-high restrictions are enforced for the rest of the population, a medium restriction reduction for VP holders leads to an epidemic that is initially overcriti-189 cal, then becomes subcritical and after a few months switches to overcritical again, starting a new wave 190

of infections (orange curve in Fig. 1c; denoted +-+, this is also the scenario shown in the simulation in Fig. 1b). Finally, always with mid-high restrictions enforced for the rest of the population, a low restriction reduction for VP holders leads to an epidemic that is initially overcritical and then switches to subcritical (another example of scenario +-, cyan curve in Fig. 1c).

In each scenario we computed the time evolution of the *instantaneous doubling time* D, capturing how fast the infections grow. For a given f, D(t) is the doubling time that would be observed for the growth of a small initial number of infections at time t, with enforced restrictions f. Very short doubling times, below 30 days, can be observed in three scenarios that are (eventually) overcritical: see the red, orange and pink curves in the Supplementary Fig. S1.

Flexible measures are required to avoid epidemic resurgence depending on parameter setups

The relevant $f - f_v$ parameter space, where $f_v \leq f$, can be divided into five regions, where the epidemic 202 dynamics follows the distinct patterns exemplified in Fig. 1c. Fig. 2 shows the impact of changing 203 specific single parameter values on the expected scenarios and on times to critical events, tracking time 204 up to two years. The area occupied by each region changes depending on the parameter setups. For 205 example, in the reference setup for the Delta variant (a = 0.79 - the Comirnaty effectiveness on the 206 Delta variant, $v=v_r=0.004,\, d=0.12$ - the fraction of never vaccinated in the United Kingdom, 207 $\omega = 1/500$, $\kappa = 1/500$, and proportional mixing) in Fig. 2a, the overcritical region (denoted +, with 208 R^* always above 1) occupies the lower left corner. This region is enlarged in the case of a lower vaccine 209 effectiveness (a = 0.6 - the effectiveness of Vaxzevira on the Delta variant, Fig. 2b), and higher waning 210 rate (Fig. 2f). In contrast, it shrinks with a higher vaccination rate (Fig. 2c), indicating that there is 211 a concrete benefit from deploying efficient vaccination programs. The subcritical region (-, with R^* 212 always smaller than 1) lies in the opposite corner of the $f - f_v$ space, for larger restriction values, and, 213 for a fixed fraction of never-vaccinated d, tends to decrease for setups where the overcritical region 214 increases. As expected, the switch to a larger fraction of never-vaccinated (to d = 30%, corresponding 215 to the reported fraction in France), increases the overcritical (+) region (Fig. 2e). But, at the same time, 216 the larger fraction of never-vaccinated increases also the subcritical (-) region. This is due to the fact that 217 the never-vaccinated are assumed to follow stricter restrictions, compared to VP holders, and therefore 218 their larger fraction can constrain the emergence of the later waves, characteristic of the regions +-+ and -+. Still, a strategy relying on this effect might be difficult to implement due to the large + region and 220 can lead to undesirable outcomes in practice. 221

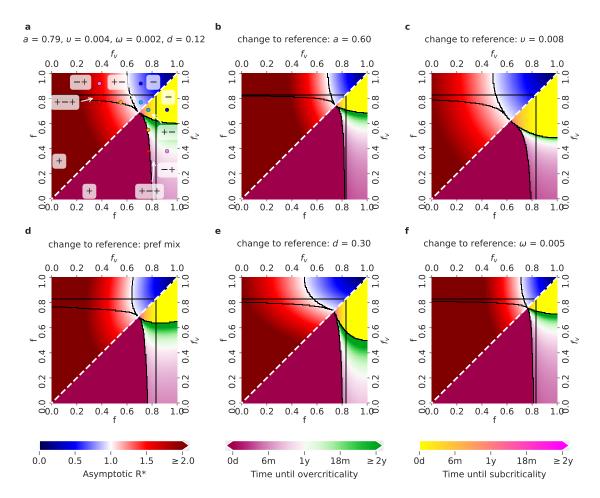


Figure 2: Possible COVID-19 epidemic dynamics for different parameter setups for the Delta variant. The relevant $f - f_v$ parameter space, where $f_v \leq f$, can be divided into five regions (delimited by black borders), each associated with a different behavior of the epidemics. On the diagonal (white dashed line), $f = f_v$, i.e., the restrictions for VP holders and for the rest of the population are the same - corresponding to the situation when VPs are not introduced at all. Lower triangles show the time until the last critical threshold: different colour scales correspond to the time until the switch either from a subcritical to an overcritical epidemic (time until overcriticality, violet-green scale), or from an overcritical to a subcritical epidemic (time until subcriticality, yellow-pink scale). Upper triangles show the asymptotic R^* , as a function of the values of f and f_v (blue-red scale, with blue associated with $R^* < 1$ and red associated with $R^* > 1$). a. Reference setup, with a = 0.79 (corresponding to the effectiveness of the Comirnaty vaccine on the Delta variant), $v = v_r = 0.004$, $\omega = 0.002$, d = 0.12 (fraction of never-vaccinated in the United Kingdom) and proportional mixing. The choices of (f, f_v) corresponding to the five scenarios exemplified in Fig. 1c are denoted by points of the same colour. **b**. Setup with a decreased vaccine effectiveness: a = 0.6 (corresponding to the effectiveness of the Vaxzevria vaccine on the Delta variant). c. Setup with an increased vaccination rate: $v = v_r = 0.008$. d. Setup with preferential (instead of proportional) mixing e. Setup with an increased fraction of people who will not get vaccinated: d = 0.3 (fraction of never-vaccinated in France). f. Setup with an increased waning rate: $\omega = 1/200$.

Inside each of the three regions associated with the +-+, -+, +- scenarios in Fig. 1c, the specific parameter settings differ by the time to the critical threshold of interest for that region (the last observed switch between subcritical and overcritical epidemic, which for the +-+ region, for example, is the second critical threshold; see Methods for the computation of the times to critical thresholds). For

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the reference setup (Fig. 2a) and the +-+ region, the critical threshold is reached after a minimum \sim 4 months. Decreasing the vaccine effectiveness from Comirnaty's to Vaxzevira's (Fig. 2b), as well as in-creasing the waning rate (Fig. 2f), leads to overcriticality sooner, after a minimum of \sim 2 and \sim 3 months respectively, for low f_v values. Increasing vaccination rate (Fig. 2c) shrinks the +-+ region. The com-parison between proportional and preferential mixing shows the impact of more intense interactions of the VP holders inside of their own group, and less intense contacts of the VP holders with the rest of the population. With preferential mixing (Fig. 2d), the +-+ region becomes larger and overcriticality is reached even sooner. This is due to the fact that preferential contacts among VP holders accelerate the emergence of the wave caused by infections of the VP holders. Seemingly counter-intuitively, increasing the number of never-vaccinated people (Fig. 2e) shrinks the +-+ region and delays the onset of overcrit-icality. This is due to the fact that the onset of overcriticality in the +-+ region depends not only on the intensity of contacts of the VP holders, but also on their fraction in the population; with a larger fraction of never-vaccinated, the fraction of VP holders in the population decreases.

The above analysis of the different regions predicts a possible switch to overcritical epidemic growth for a given parameter setup and, if there is a switch, it provides the time it happens, counting from the onset of the vaccination program. It does not, however, indicate how fast the overcritical growth will be. To inform about what growth rates can be eventually expected in the overcritical regime, we compute the asymptotic R^* (the $R^*(t)$ for $t \to \infty$, see Methods) for all parameter setups and all combinations of restrictions in the relevant $f - f_v$ space. For a given restriction combination \mathbf{f} , the asymptotic R^* indicates how quickly the infections grow shortly after the restrictions are set to \mathbf{f} in the asymptotic state. For all considered parameter setups, except for the one with high (re-)vaccination rate, and for all except the +- and the - regions, large asymptotic R^* can be expected, which corresponds to short doubling times (Fig. 2). This analysis highlights the importance of avoiding the overcritical (+) region, as there the asymptotic R^* values can even exceed 2 when the restrictions are low.

Comparing Figure 2 to Supplementary Figure S2 shows how the Delta variant worsens all scenarios with respect to the Alpha variant: in all panels of Figure 2, the Delta variant leads to a considerable expansion of the overcritical region, shrinking of the safe subcritical region, and to consistently larger values of asymptotic R^* . This is due not only to a higher transmissibility of the Delta variant, but also due to the fact that the considered vaccines have lower effectiveness for this variant, as compared to the Alpha variant.

We further investigate how the expected scenarios, times to critical events (tracking time up to two years), and asymptotic R^* values are affected by changes of two parameters at once, compared to the

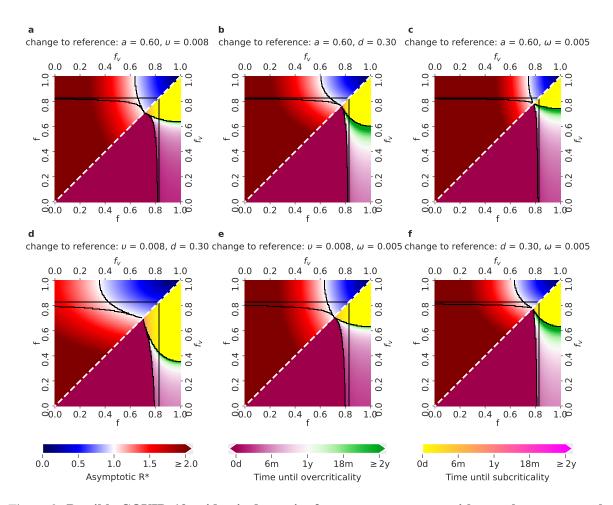


Figure 3: Possible COVID-19 epidemic dynamics for parameter setups with two changes w.r.t. the reference setup, for the Delta variant (changes as in Table 1, rows 6-11) Colors of the lower triangles correspond to the time until critical changes in epidemic dynamics, while the colors of the upper triangles correspond to the values of asymptotic R^* , as in Fig. 2 a. Setup with decreased effectiveness a=0.60 (corresponding to the effectiveness of the Vaxzevira vaccine on the Delta variant), and increased (re-)vaccination rates $v=v_r=0.008$. b. Setup with decreased a=0.60 and increased fraction of never vaccinated d=0.30 (corresponding to the change from the fraction of never-vaccinated in the United Kingdom to the fraction of never-vaccinated in France). c. Setup with decreased a=0.60 and increased waning rate $\omega=0.005$. d. Setup with increased $v=v_r=0.008$ and increased $v=v_r=0.008$. Setup with increased $v=v_r=0.008$.

reference setup, for the Delta (Fig. 3) and the Alpha variant (Supplementary Fig. S3). The double parameter changes give insight into the possible synergistic and compensatory effects between individual parameter changes. Compared to the effect of only decreasing the vaccine effectiveness from Comirnaty's to Vaxzevira's (Fig. 2b), the effect of jointly decreasing the vaccine effectiveness and increasing the vaccination rate (Fig. 3a) indicates that a higher vaccination rate can compensate to some extent for the loss of effectiveness. Similarly, an increased vaccination rate can counteract increased immunity waning rate (Fig. 3e). The combination of decreased effectiveness and increased immunity waning rate has the worst effect, as it largely increases the overcritical region (+), decreases the subcritical region

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(-) and accelerates the times to the overcriticality in all other regions (Fig. 3c). Finally, combinations of an increased never-vaccinated fraction with other parameter changes show an interesting mix of effects. When both the never-vaccinated fraction and the vaccination rate increase, the overcritical (+) region decreases and the subcritical region increases, while the times to overcriticality in the +-+ and the -+ regions increase (Fig. 3d). Similarly, there is a synergistic effect of the combination of the increased never-vaccinated fraction and the increased immunity waning rate (Fig. 3f). For the Alpha variant, the effects of coupled parameter changes combine the same way as for the Delta variant, but once again it is apparent that, for all the parameter setups we considered, with the Alpha variant much less restrictions are required to avoid epidemic resurgence than with the Delta variant (Supplementary Fig. S3).

Taken together, these results indicate that, unless novel vaccines with higher effectiveness are invented and distributed, and unless much faster and wider vaccination programs are implemented, resulting in much more favorable parameter settings than the realistic ones analysed here (including those considered optimistic), highly unfavorable infection dynamics are likely to emerge for the Delta variant, and less, but still, for the Alpha variant. The -+ and +-+ regions in Figures 2 and 3 can seem attractive as restriction policies, because they entail larger freedom for the VP holders; both these regions, however, eventually result in epidemic resurgence and either should be avoided or the time spent in these regions should be very carefully regulated. For example, if sufficient restrictions are enforced for the rest of the population, the VP holders may initially be granted additional freedoms (larger if the Alpha variant is dominant in the population, and much lower if the Delta variant is dominant), which corresponds to the -+ region. In this way, an overcritical situation (region +) will be avoided. However, to prevent the epidemic from becoming overcritical after an initial decline in case numbers, restrictions on VP holders need to be timely increased and adapted, to avoid spending longer time in the -+ region than the time to overcriticality. Thus, moving out of the -+ region to the +- region with the right timing could be one of possible strategies. It may, however, be more practical to circumvent many changes of restriction policies over time and it may be fair for everyone to face the same restrictions. Safe common restrictions, however, corresponding to the parameters on the diagonal in the subcritical (-) region or Figures 2 and Fig. 3 and Supplementary Figures S2 and Fig. S3, are relatively high, especially those required by the Delta variant, and may therefore cause unrest in the population.

A minimum common restriction level can keep the epidemic subcritical in the long-term

We compute the minimum common restriction level f_{\min} for the whole population that would guarantee to avoid an overcritical epidemic in the long-term (for time approaching infinity, Methods):

$$f_{\min} = \max(0, 1 - 1/(R_{\max} \cdot (1 - V^{\mathrm{as}})),$$

where V^{as} as is the asymptotic fraction of the immunized in the population

$$V^{\rm as} = (1 - d) \frac{a}{1 + \omega/\nu_r}.$$

The resulting values differ depending on the setups of vaccine effectiveness a, revaccination rate v_r , 298 the fraction of never-vaccinated population d and immunity waning rate ω (Tab. 1). The minimum 299 common restrictions for the reference setup are equal to $f_{\min} = 0.69$. Out of parameter setups with 300 single change compared to the reference, doubled (re-)vaccination speed leads to the lowest possible 301 common restriction level. Even for this most optimistic setup (high a=0.79, high $v_r=0.008$, low 302 d=0.12, low $\omega=0.002$; Tab. 1 third row) we obtain $V^{\rm as}=0.6$, and $f_{\rm min}=0.62$. The level of 303 0.62 restrictions is around twice as high as the level 0.29 that would be required for the Alpha variant 304 (Supplementary Tab. 1), and is a considerable reduction of freedom compared to before the pandemic. It 305 is noteworthy that in the long term, to avoid infections rising, minimum common restrictions have to be 306 increased to 0.74 with the larger fraction of never vaccinated d. Thus, a scenario with a large fraction of 307 the population without immunity gained via vaccination requires long-term high restriction levels, and 308 as such seems politically unfeasible. 309 When changing two parameters simultaneously in order to assess synergies, we find that a decreased 310 vaccine effectiveness or an increased share of never vaccinated or an increased waning rate can barely 311 be offset by an increase in vaccination speed. Both a decreased vaccine effectiveness and an increase 312 in the share of never vaccinated in combination with an increased waning rate considerably increase the 313 minimum restriction level that is adequate to ensure resurgence can be avoided. The latter (increased 314 d, increased ω as compared to the reference) is the most pessimistic of the considered scenarios, with 315 $f_{\min} = 0.8$. 316 This analysis highlights the importance of vaccine effectiveness, vaccination speed, but also of the 317 fraction of the never-vaccinated. Such demanding requirements for stringent minimum common restric-318 tions could be reduced if novel vaccines with higher effectiveness become available, if faster and wider 319

	Parameter setup	a	v_r	d	ω	V^{as}	f_{\min}
1	Reference setup (ref Fig. 2a)	0.79	0.004	0.12	0.002	0.46	0.69
2	Decreased a (ref Fig. 2b)	0.6	0.004	0.12	0.002	0.35	0.74
3	Increased v_r (ref Fig. 2c)	0.79	0.008	0.12	0.002	0.56	0.62
4	Increased d (ref Fig. 2e)	0.79	0.004	0.3	0.002	0.37	0.74
5	Increased ω (ref Fig. 2f)	0.79	0.004	0.12	0.005	0.31	0.76
6	Decreased a and increased v_r (ref Fig. 3a)	0.6	0.008	0.12	0.002	0.42	0.71
7	Decreased a and increased d (ref Fig. 3b)	0.6	0.004	0.3	0.002	0.28	0.77
8	Decreased a and increased ω (ref Fig. 3c)	0.6	0.004	0.12	0.005	0.23	0.78
9	Increased v_r , increased d (ref Fig. 3d)	0.79	0.008	0.3	0.002	0.44	0.70
10	Increased v_r , increased ω (ref Fig. 3e)	0.79	0.008	0.12	0.005	0.43	0.71
11	Increased d , increased ω (ref Fig., 3f)	0.79	0.004	0.3	0.005	0.18	0.80

Table 1: Asymptotic level of immunization $V^{\rm as}$ and minimum common restrictions $f_{\rm min}$ for the Delta variant and different parameter setups, for parameters: vaccine effectiveness a, revaccination rate v_r , fraction of never-vaccinated d, and waning immunity rate ω . The first row concerns the reference setup; rows below are setups with the same parameters as in the reference setup, but with either one parameter changed (in bold; rows 2–5; same as in Figures 2 and 4, apart from preferential mixing, as it is not relevant for common restrictions) or two parameters changed (in bold; rows 6–11).

vaccination programs are implemented, and finally, if the never-vaccinated fraction shrinks.

Endemic state analysis reveals the possibility of large daily infection numbers

For a given restriction combination \mathbf{f} , the above analyzed asymptotic instantaneous reproduction number R^* (Figures 2 and 3, Supplementary Figures S2 and S3) indicates how quickly the infections grow shortly after the restrictions are set to \mathbf{f} in the asymptotic state; however, it does not provide insight into the daily infection numbers the system converges to. To this end, we compute the daily infection numbers both in the vaccinated and the unvaccinated subpopulations in the endemic state, as functions of the restrictions \mathbf{f} for the Delta variant (Fig. 4) and compare it to the scenarios achieved with the Alpha variant (Supplementary Fig. S4). In contrast to the computation of the instantaneous reproduction number R^* and its asymptotic values, which is based on the analysis of the linearized system of the ordinary equations in the VAP-SIRS model, the endemic state is based on the computation of the stationary point of the full set of the equations (Methods).

For all parameter setups, in all regions apart from the subcritical (–) region, the daily infections in the endemic state will exceed 10 per million, which is the tolerance threshold for efficient test, trace and isolation policy [52]. For the setups that correspond to low vaccination effectiveness or short waning time, the endemic state is most unfavorable, as the daily infections can exceed 1000 daily cases per million. A high (re-)vaccination rate is crucial to expand the safe region (Fig. 4c). A sharp transition can be seen between favorable and unfavorable parameter setups. In the endemic state, the daily infection numbers

in the vaccinated subpopulation can exceed that of the unvaccinated subpopulation, which underlines the risks of waning immunity.

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Considering the parameter setups that arise by changing two parameters at once with respect to the reference setup gives insights about their joint effects, shown in Fig. 5; the effect of simultaneous parameter variations is akin to that described earlier for the values of asymptotic R^* and time to critical thresholds in Figure 3.

Again, comparison with the endemic infection numbers predicted for the Alpha variant (Supplementary Fig. S4 and Supplementary Fig. S5) shows that Delta has considerably narrowed opportunities to

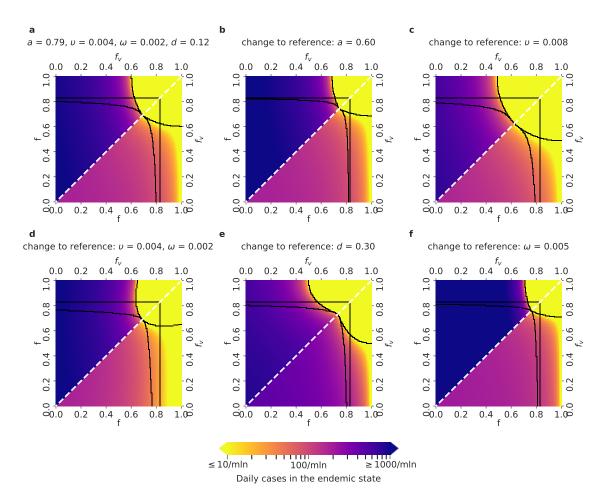


Figure 4: **Daily COVID-19** infection cases in the endemic state for different parameter setups and the **Delta variant.** Lower triangles show the daily infection numbers in the unvaccinated, and upper triangles in the vaccinated population in the endemic state of the epidemics, for the relevant $f - f_v$ parameter space, where $f_v \le f$. Black borders delineate the five regions identified in Figures 2 and 3. Parameter setups as in Figure 2: **a.** Reference setup, with a = 0.79 (corresponding to the effectiveness of the Comirnaty vaccine on the Delta variant), $v = v_r = 0.004$, $\omega = 0.002$, d = 0.12 (fraction of never-vaccinated in the United Kingdom) and proportional mixing. **b.** Setup with a decreased vaccine effectiveness: a = 0.6 (corresponding to the effectiveness of the Vaxzevria vaccine on the Delta variant). **c.** Setup with an increased vaccination rate: $v = v_r = 0.008$. **d.** Setup with preferential (instead of proportional) mixing **e.** Setup with an increased fraction of people who will not get vaccinated: d = 0.3 (fraction of never-vaccinated in France). **f.** Setup with an increased waning rate: $\omega = 1/200$.

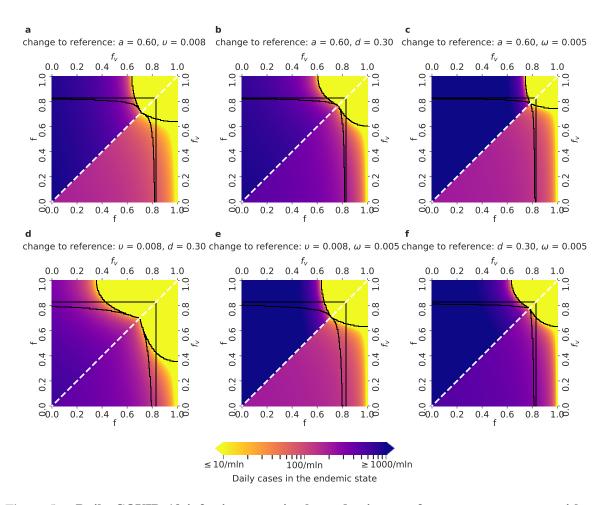


Figure 5: **Daily COVID-19** infection cases in the endemic state for parameter setups with two changes w.r.t. the reference setup, and the Delta variant. Lower triangles show the daily infection numbers in the unvaccinated, and upper triangles in the vaccinated population in the endemic state of the epidemics, for the relevant $f - f_v$ parameter space, where $f_v \le f$. Black borders delineate the five regions identified in Figures 2 and 3. Parameter setups as in Figure 3: **a.** Setup with decreased effectiveness a = 0.60 (corresponding to the effectiveness of the Vaxzevira vaccine on the Delta variant), and increased (re-)vaccination rates $v = v_r = 0.008$. **b.** Setup with decreased a = 0.60 and increased fraction of never vaccinated d = 0.30 (corresponding to the change from the fraction of never-vaccinated in the United Kingdom to the fraction of never-vaccinated in France). **c.** Setup with decreased a = 0.60 and increased waning rate a = 0.005. **d.** Setup with increased a = 0.008 and increased a = 0.008 and increased a = 0.008. Setup with increased a = 0.008 and increased a = 0.008. Setup with increased a = 0.008. Setup with increased a = 0.008. Setup with increased a = 0.008.

reduce restrictions for the VP holders, underlining the negative impact of the higher transmissibility of
the Delta variant and lower effectiveness of the vaccines on this variant.

Discussion

Introducing VPs is widely seen as a means to opening up economies and societies, despite the ongoing epidemic. A recent complication in this respect is the rise of the Delta variant with its higher transmissibility and decreased vaccine efficacy. To inform this discussion, we extend a SIR model to reflect

vaccination dynamics and possibly different restrictions for VP holders, with empirical parameters for both the Alpha and Delta variant.

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VAP-SIRS deliberately keeps several aspects simple. The model is not compartmentalized for age groups and does not explore the impact on hospitalisation or intensive care unit utilization like some other 355 models, albeit in the context of exploring different parameters than larger freedom for VP holders [27, 356 29, 31, 32, 33, 34]. Deaths could be taken into account through a straightforward modification of the 357 model, which would however lead to more parameters. In this case, the fact that vaccination reduces 358 the risk of death would have to be accounted for. The impact of deaths, need for intensive care, or 359 long-COVID cases on public health and society, which is very important especially when the epidemic 360 becomes overcritical, can be indirectly assessed on the basis of the number of cases. In general, features such as age groups do not add further insights into the questions which are the focus of our study, 362 namely, the impact of VPs on infection dynamics and the parameters that increase the risks of overcritical 363 dynamics, given the spread of the Delta variant. In this context, the advantage of our model is that it is 364 enriched in features such as revaccinations and waning immunity, which are particularly relevant in the 365 long term. Avoiding another wave is a prudent goal due to the threats it poses, in the form of long-term 366 health effects, the deleterious impact on societies and the emergence of new variants. 367

Nevertheless, possible extensions to our model could include inter- individual or age-dependent variations in immunity, which would render it relevant for people with severe chronic conditions or immunodeficiencies. The presented analysis has been performed assuming that without restrictions, the maximum reproduction number of the virus is $R_{\text{max}} = 6$ or $R_{\text{max}} = 4$ for Delta and Alpha variants, respectively. More transmissible variants could easily be modeled by fixing higher values of R_{max} . Possible future variants, for which existing vaccines may potentially be less effective could be considered using our model by fixing smaller vaccine effectiveness parameter a than the values we considered. We also do not account for seasonality, which seems to have a dampening effect on epidemic dynamics during the summer months, when it is possible to temporarily reduce restrictions. Not all analyzed parameter values are exactly known, such as the post-vaccination or natural immunity waning time. We, however, fix optimistic values for such parameters, and show that unfavorable infection dynamics can still be obtained even under optimistic assumptions.

Despite limitations, our model accounts for key parameters influencing infection dynamics and gives valuable insights into policies pertaining to the introduction of VPs, contributing to render the valid goal of avoiding resurgence attainable. We find that a wide range of the VAP-SIRS model parameter choices, even optimistic ones, show the possibility of an epidemic resurgence for both variants. The risk of resurgence is higher in the case of implemented VP, i.e., with VP holders enjoying reduced restrictions, such as being exempt from wearing masks and testing before entering business, gastronomical, or tourist premises. The resurgence can be avoided in the short and in the long run only when the restrictions are kept high for the rest of the population, and the reduction for the VP holders is moderate or small, especially for the Delta variant. The main driver of this phenomenon is the potential lack of immunity of VP holders. With a VP, people enjoy lower restrictions, while some actually remain both susceptible and potentially contagious because the vaccine was ineffective or the immunity has waned.

For all analyses, a comparison between values for the Alpha and Delta variants shows that Delta has drastically worsened all scenarios. One illustrative finding is that the minimum level of common restrictions to avoid resurgence in the reference setup has doubled from a low 0.29 (Alpha) to medium 0.62 (Delta).

Changing key parameters such as vaccine effectiveness, (re-)vaccination rate, or waning immunity rate to realistic levels found in studies or certain countries shows the expected effect these changes would have on infection dynamics. We quantified these effects by evaluating the times to overcriticality, asymptotic instantaneous reproduction number R^* , minimum necessary common restriction level that avoids resurgence in the long term, and numbers of cases per million in the endemic state, for the relevant range of possible restrictions for the VP holders and the rest of the population. As expected, the model shows that there is a larger selection of admissible restrictions' combinations under high vaccine effectiveness, low share of never vaccinated, a higher (re-)vaccination rate, slowly waning immunity, and proportional social mixing. For the Delta variant, however, and even for optimistic of these parameter setups, the room for manoeuvre in terms of lowering the restrictions is very small. Moreover, not all of these parameters are amenable to policy action. In a nutshell, our results consistently suggest that with the Delta variant and with the way the vaccination program and introduction of VPs is currently implemented, unfavourable developments of the epidemic are likely, and to counteract these developments and to maximize possible freedoms for their citizens, decision makers should exploit all possibilities to enhance the development of effective vaccines, increase vaccination speed and the number of vaccinated.

It is noteworthy that VP holders are less likely to be tested, as they are assumed to be protected and they may exhibit milder symptoms. Therefore, their potential infection is more likely to remain undetected, resulting in an effect similar to that of lowering restrictions. To prevent undesirable outcomes, the testing and quarantine criteria should be applicable also to the VP holders. Testing should aim at detection of vaccinated people that have lost, or have never gained, immunity. Finally, temporary VPs could be considered, with their prolongation conditioned on high antibody level or recent (re-)vaccination.

The utilisation of tools such as the VAP-SIRS model, along with different tools available to policymakers should be explored in the context of monitoring the implementation of VPs, including the EU

DCC measures, to ensure optimisation of key parameters. In this manner, evidence-informed policymaking would be safeguarded as would the best possible outcomes in terms of effectively combatting
the current pandemic.

We introduce a modified susceptible-infectious-recovered-susceptible (SIRS) model [39] (Fig. 1a). The

421 Methods

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Mathematical model

population is divided into two subpopulations: those who are not vaccinated (S, I, R) and those who 424 got vaccinated at least once (S_V, I_V, R_V, V) . We assume that the group of non-vaccinated susceptible 425 individuals S (and, similarly, infected I and recovered R) is divided into two subgroups: S_N and S_D . 426 The S_N compartment contains such susceptible who will eventually be vaccinated, while those in S_D 427 will not. The S_N population is vaccinated with rate v and effectiveness a. Consequently, the individuals from 429 the S_N group populate the vaccinated group V with rate av. The individuals in V are considered immune, 430 and we assume that immunization prevents them both from getting infected and infecting others. The 431 S_V compartment is composed of S_1 and S_2 (and, similarly, vaccinated infected I_V consists of I_1 and 432 I_2). Due to vaccine ineffectiveness, people in S_1 are perceived as immunized, but in fact are susceptible. S_1 is populated from S_N with rate (1-a)v. The vaccinated from the V group move to the S_2 group of 434 susceptibles with immunity waning rate ω . The individuals from the S_1 group move to S_2 with the same 435 rate ω . The S_2 group is the group of vaccinated, but no longer immune, and thus, susceptible individuals. 436 In contrast to S_1 , we consider that the S_2 group is subject to revaccination. Consequently, a fraction of 437 size a of the population from S_2 populates V with rate av_r and a fraction of size (1-a) populates S_1 438 with rate $(1-a)v_r$. Across the manuscript, we assume $v_r = v$, but the model is general and different values can be considered. Individuals from S_1 move to S_2 with rate ω to ensure that the ineffectively 440 vaccinated are revaccinated with the same speed as the ones for which the vaccine was effective. 441 Some of the susceptibles in S_1 (or, similarly, S_2) may not get revaccinated fast enough and may 442 become infected and populate I_1 (or, I_2). Then, as in the classical SIRS model, the I_1 (or I_2) population 443 recovers and populates group R_V with rate γ . We consider that the recovered in R_V may also lose the immunity, and become susceptible again and move to S_2 with rate κ . The remaining susceptible 445

- subgroups (the S_N and S_D) may undergo the same classical dynamics, i.e., become infected, recover,
- and either become susceptible again or, in case of the recovered in the R_N subgroup, become vaccinated
- 448 with rate v.
- The following parameters are used to describe population dynamics in the model:

 $f_{\rm v}, f$: restrictions level (for VP holders and others)

 β_0 : basic transmission rate

 $\beta_{\rm v}, \beta$: transmission rate (for VP holders and others)

 γ : recovery rate

 κ : natural immunity waning rate

a: vaccination effectiveness

v: vaccination rate

 v_r : revaccination rate

 ω : vaccine-induced immunity waning rate

d: fraction of population that will never get vaccinated

Finally, the following set of ordinary differential equations (ODEs) defines the dynamics

$$\frac{d}{dt}S_{D} = -(\beta I + \beta I_{V})S_{D} + \kappa R_{D},$$

$$\frac{d}{dt}S_{N} = -(\beta I + \beta I_{V})S_{N} - vS_{N} + \kappa R_{N},$$

$$\frac{d}{dt}S_{1} = v_{r}(1 - a)S_{2} + v(1 - a)S_{N} - \omega S_{1} - (\beta I + \beta_{v}I_{V})S_{1},$$

$$\frac{d}{dt}S_{2} = -v_{r}S_{2} + \omega V + \omega S_{1} - (\beta I + \beta_{v}I_{V})S_{2} + \kappa R_{V},$$

$$\frac{d}{dt}V = vaS_{N} + v_{r}aS_{2} - \omega V + v_{r}R_{V} + vR_{N},$$

$$\frac{d}{dt}I_{D} = (\beta I + \beta I_{V})S_{D} - \gamma I_{D},$$

$$\frac{d}{dt}I_{N} = (\beta I + \beta I_{V})S_{N} - \gamma I_{N},$$

$$\frac{d}{dt}I_{1} = (\beta I + \beta_{v}I_{V})S_{1} - \gamma I_{1},$$

$$\frac{d}{dt}I_{2} = (\beta I + \beta_{v}I_{V})S_{2} - \gamma I_{2},$$

$$\frac{d}{dt}R_{V} = \gamma I_{V} - \kappa R_{V} - v_{r}R_{V},$$

$$\frac{d}{dt}R_{D} = \gamma I_{D} - \kappa R_{D},$$

$$\frac{d}{dt}R_{N} = \gamma I_{N} - \kappa R_{N} - vR_{N},$$

where also the following relations hold

$$S_V = S_1 + S_2,$$

 $I_V = I_1 + I_2,$
 $S = S_D + S_N,$
 $I = I_D + I_N,$
 $R = R_N + R_D,$

with the constraint $S, S_V, I, I_V, R, R_V \ge 0$. Finally, to consider the subpopulation dynamics in terms of

fractions of the entire subpopulation, we set

$$S + S_V + I + I_V + R + R_V + V = 1 (2)$$

and denote d to be the fraction of the never-vaccinated population

$$d = S_D + I_D + R_D.$$

Modeling restrictions 454

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We assume that the VP holders consist of the following subpopulations of vaccinated at least once: 455 V, S_V, I_V, R_V . Recall that the net effect of all non-pharmaceutical interventions is modeled using pa-456 rameters f_v and f, called restrictions throughout the text. The parameter f_v amounts to the level of 457 restriction of contacts, and thus the ability to infect, within the group of VP holders. The parameter f 458 satisfies $f \geq f_{\rm v}$ and corresponds to restriction of contacts within the rest of the population, as well as 459 between the VP holders and the rest of the population. 460 The restriction level f_v for the VP holders is introduced in the model as a modulator of the trans-461 mission rate β_v . Specifically, we assume that $\beta_v = \beta_0 (1 - f_v)$, where β_0 is the transmission rate of the 462 SARS-CoV-2 virus without restrictions. We assume f_v ranges from 0 to 1, where $f_v = 0$ corresponds 463 to no restrictions enforced on the VP holders, and $f_{\rm v}=1$ corresponding to full restrictions. Given that 464 for $f_{\rm v}=0$ the reproduction number $R_{\rm max}=\beta_0/\gamma$, and that the recovery rate $\gamma=1/6$, we obtain the 465 no-restriction transmission rate $\beta_0=R_{\rm max}/6$. Thus, for the Delta variant, with $R_{\rm max}=6$, $\beta_0=1$ 466 Similarly, the transmission rate parameter $\beta = \beta_0(1-f)$ describes the transmission rate within the 467 rest of the population and between VP holders and the rest, given the restrictions f.

Proportional versus preferential types of social mixing 469

The above described model equations are based on the assumption that the social mixing between social 470 groups in the population is proportional to the group sizes (the mass action principle). Instead, prefer-471 ential mixing can be assumed, where the VP holders are more likely to contact other VP holders, since 472 they have lower restrictions [53]. This preferential bias is proportional to the difference between the restrictions f and f_v . To incorporate the preferential mixing effect in the ODE model (Equation 1) we 474 rescale the interaction terms according to the following rules: 475

$$S_V I_V \rightarrow \frac{\beta_{\rm v}}{\beta(S+I+R)+\beta_{\rm v}(1-(S+I+R))} S_V I_V$$

 $SI_V \rightarrow \frac{\beta}{\beta(S+I+R)+\beta_{\rm v}(1-(S+I+R))} SI_V,$

where S + I + R is the non-immune population.

477 Model simulations

For simulations, we solve the model numerically by means of joint Adams' and BDF methods, as im-478 plemented in the R package deSolve, Isoda method of the ode function [54]. The method monitors data 479 in order to select between non-stiff (Adams') and stiff (BDF) methods. It uses the non-stiff method 480 initially [55]. 481 To generate the data presented in Figure 1b, we use the reference setup of parameters for the Delta 482 variant: $\beta_0 = 1$, f = 0.77 (and thus $\beta = 0.23$), $f_v = 0.55$ (and thus $\beta_v = 0.45$), $\gamma = 1/6$, $\kappa = 1/500$, $a=0.79, \, \upsilon=\upsilon_r=1/250, \, \omega=1/500, \, d=0.12,$ with initial conditions $I=10^{-6}, \, I_D=d\cdot I=10^{-7};$ 484 $I_N = (1-d) \cdot I = 0.9 \cdot 10^{-6}$, R = 0, V = 0. Given I(t) resulting from the solution of the model's 485 ODE system, to present the final results as easier interpretable cases per million rather than fractions, 486 we re-scale the results by 1M. Additionally, we compute a proxy for the daily incidence number of new 487 cases from the following relation between I(t) and $I^*(t)$:

$$\begin{split} I\left(t\right) &= \int_{0}^{t} e^{-\gamma(t-\tau)} I^{*}\left(\tau\right) d\tau \\ &= \int_{t-1}^{t} e^{-\gamma(t-\tau)} I^{*}\left(\tau\right) d\tau + e^{-\gamma} \int_{0}^{t-1} e^{-\gamma(t-1-\tau)} I^{*}\left(\tau\right) d\tau \\ &\simeq \frac{1}{\gamma} I^{*}\left(t\right) \left(1 - e^{-\gamma}\right) + e^{-\gamma} I\left(t - 1\right). \end{split}$$

Thus, the $I^*(t)$ is computed as

$$I^*(t) \simeq \frac{\gamma}{1 - e^{-\gamma}} \left(I(t) - e^{-\gamma} I(t-1) \right).$$

We proceed similarly to obtain daily incidence numbers I_1^* , I_2^* and for the sum of all infected, and again to make it interpretable in the figures we re-scale it by 1M.

492 Stability analysis

- The vaccination dynamics can be solved explicitly in the absence of infections. Fixing $I=I_V=R=$
- 494 $R_V = 0$, and assuming $v = v_r$, we obtain

$$S(t) = d + (1 - d) e^{-vt},$$

$$V(t) = (1 - d) \frac{va}{va + \omega} \left(1 - e^{-(va + \omega)t} \right),$$

$$S_V(t) = 1 - S - V.$$

For convenience, where it is not needed, we drop the time argument.

Taking an adiabatic approach we linearize the infection dynamics for small I, I_V and R under the assumption of slowly varying S, S_V and V. In that case, the infection dynamics decouples from the vaccination dynamics and the Jacobian submatrix J_{sub} for the equations for I and I_V is given by:

$$J_{sub} = \begin{pmatrix} \beta S - \gamma & \beta S \\ \beta S_V & \beta_V S_V - \gamma \end{pmatrix}.$$

Given the Jacobian submatrix, we can approximate the dynamics in a small neighborhood of the I=

497 $I_V = 0$ state as

$$\begin{pmatrix} \frac{d}{dt}I\\ \frac{d}{dt}I_V \end{pmatrix} = \begin{pmatrix} \beta S - \gamma & \beta S\\ \beta S_V & \beta_V S_V - \gamma \end{pmatrix} \cdot \begin{pmatrix} I\\ I_V \end{pmatrix}. \tag{3}$$

The instantaneous reproduction number R^* and the instantaneous doubling time D

Since the largest and the second largest eigenvalues λ_{\max} and λ_2 of J_{sub} are both real, the solution to Equation 3 providing the dynamics of infection numbers of the vaccinated and the rest of the population in time can be written in the following form

$$\begin{pmatrix}
I(t) \\
I_V(t)
\end{pmatrix} = c_1 w_1 e^{\lambda_{\text{max}} t} + c_2 w_2 e^{\lambda_2 t} = e^{\lambda_{\text{max}} t} (c_1 w_1 + c_2 w_2 e^{(\lambda_2 - \lambda_{\text{max}})t}), \tag{4}$$

where w_1 and w_2 are the respective eigenvectors, and c_1 and c_2 are constants depending on the initial conditions.

Since we have $\lambda_2 - \lambda_{\text{max}} \leq 0$, we can approximate the time evolution of infection numbers by

$$\begin{pmatrix} I(t) \\ I_V(t) \end{pmatrix} \approx c_1 w_1 e^{\lambda_{\text{max}} t}. \tag{5}$$

The largest eigenvalue of J_{sub} is given by

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$$\lambda_{\text{max}} = \frac{1}{2}S\beta - \gamma + \frac{1}{2}S_V\beta_v + \frac{1}{2}\sqrt{S^2\beta^2 + S_V^2\beta_v^2 - 2SS_V\beta\beta_v + 4SS_V\beta^2},$$
 (6)

whereby it is convenient to express λ_{\max} as a function of $R_1 = \frac{\beta}{\gamma}$ and $R_2 = \frac{\beta_v}{\gamma}$. We then obtain

$$\lambda_{\text{max}} = \gamma \left(\frac{1}{2} \left(R_1 S + R_2 S_V \right) + \frac{1}{2} \sqrt{\left(R_1 S - R_2 S_V \right)^2 + 4S S_V R_1^2} - 1 \right). \tag{7}$$

Given the population fractions S(t) and $S_V(t)$ at a given time instant t, the linearized dynamics of infections given by Equation 3 has a corresponding two-type Galton-Watson branching process, which is a microscopic description of the dynamics. The two types of the process correspond to the I and I_V groups. The type I individuals generate $Pois(R_1S)$ offsprings of type I and $Pois(R_1S_V)$ offsprings of type I_V . The type I_V individuals generate $Pois(R_1S)$ offsprings of type I and $Pois(R_2S_V)$ offsprings of type I_V . The linearized dynamics (3) can then be understood as a mean field limit of the microdynamics described by such a branching process. Moreover, the spectral norm

$$R^* = \frac{1}{2} \left(R_1 S + R_2 S_V \right) + \frac{1}{2} \sqrt{4R_1^2 S S_V + \left(R_1 S - R_2 S_V \right)^2}$$
 (8)

of the transition matrix

$$\begin{pmatrix} R_1 S & R_1 S_V \\ R_1 S & R_2 S_V \end{pmatrix}$$

of the branching process can be interpreted as the reproduction number of the branching process, since
the expected number of infected in generation n grows like $const \cdot (R^*)^n$ [56]. We refer to R^* as the
instantaneous reproduction number. The term instantaneous comes from the fact that we are considering
the linearized adiabatic dynamics in a small neighborhood of the $I = I_V = 0$ (ref Eq. 3).

The above discrete branching process can be extended to a continuous time branching process by assuming a probability distribution on the generation time, denoted $\varphi(\gamma)$. The growth of the continuous time branching process $const \cdot e^{\alpha t}$ is characterized by its Malthusian growth parameter, denoted α . The relation between the instantaneous reproduction number R^* , the distribution $\varphi(\tau)$ and the Malthusian

parameter α for such a branching process is given by

$$R^* \cdot \mathcal{L}_{\varphi} \left(\alpha \right) = 1$$

where $\mathcal{L}_{\varphi}\left(\alpha\right)$ is the Laplace transform $\int_{0}^{\infty}e^{-\alpha\tau}\varphi\left(\tau\right)d\tau$ of the distribution φ [56]. Since the setting 518 of ODE model (1) implies exponential distribution of the generation time, i.e, $\varphi(\gamma) = Exp(\gamma)$, the 519 following relation holds: $\alpha = \gamma (R^* - 1)$. 520 By Equation 5, the Malthusian parameter α for our dynamics is given by the largest eigenvalue 521 λ_{\max} . Hence we obtain the relation between the instantaneous reproduction R^* and the λ_{\max} as $\lambda_{\max} =$ $\gamma\left(R^*-1\right)$. Note that since both S and S_V are functions of time, so are λ_{\max} and R^* . 523 It is noteworthy that in the above equations, all R_1 , R_2 , R_1S and R_2S_V , and R^* should be seen 524 as reproduction numbers, but of a different nature [57]. R_1 and R_2 are reproduction numbers taking 525 into account the restrictions f and f_v , respectively. The R_1S and R_2S_V are also group specific, but in 526 addition incorporate the respective group sizes. Finally, R^* combines all these factors together. 527 Having this and Equation 5, we define the instantaneous doubling time at time, denoted t D(t), as 528 the solution D of $e^{\gamma(R^*(t)-1)\cdot D}=2$. Such obtained doubling times are featured in Supplementary Figure 529 **S**1. 530

The times of transitions between subcritical and overcritical epidemics

The analysis of the linearized dynamics around $I=I_V=0$ allows us to determine transitions between subcritical and overcritical epidemics. Such transitions occur at the time instants t at which $\lambda_{\max}(t)=0$, or, equivalently, at $R^*(t)=1$. We thus find that for given values of S(t) and $S_V(t)$ the critical times t for transitions between subcritical and overcritical epidemics are the roots of the equation

$$\lambda_{\max}(t) = 0.$$

The obtained critical threshold times are plotted in the lower triangles of the panels in Figures 2 and 3 in the main text. In the case of proportional mixing the above equation is equivalent to:

$$(R_1S(t) - 1)(R_2S_V(t) - 1) = R_1^2S(t)S_V(t).$$

534 Asymptotic structure of the population

The asymptotic structure of the population in terms of the sizes of the subpopulations V, S_V and S_D can be easily obtained by setting $I = I_V = R = R_V = 0$ and computing the stable stationary solution for $V^{\rm as}$, $S^{\rm as}$ and $S_V^{\rm as}$ of our ODE system 1:

$$S_{V}^{as} = d$$

$$S_{V}^{as} = (1 - d) (1 - \eta)$$

$$V^{as} = (1 - d) \eta$$

$$S^{as} + S_{V}^{as} = 1 - V^{as},$$

where

$$\eta = \frac{a}{1 + \omega/\upsilon_r}$$

can be seen as the actual immunization rate in the population, and is expressed as a function of vaccine effectiveness a and the ratio of the immunity waning rate ω and the revaccination rate v_r . The obtained values correspond to the structure in the limit $t \to \infty$ and represent the structure to which the population converges in the long term.

Having this, we obtain the asymptotic instantaneous reproduction number R^* by inserting the asymptotic values S^{as} and S_V^{as} into Equation 8. These values are plotted in the upper triangles in the panels of Figures 2 and 3 in the main text.

Finally, we solve for such minimum common restrictions $f=f_{\rm v}=f_{\rm min}$, which will result in instantaneous reproduction number $R^*=1$ for the different vaccine effectiveness and vaccination rate setups. Hence $f_{\rm min}$ is found from $R_{\rm max}\left(1-f_{\rm min}\right)==\frac{1}{1-V}$ as

$$f_{\min} = \max\left(0, 1 - \frac{1}{R_{\max}(1 - V^{\mathrm{as}})}\right).$$

545 Endemic state

The endemic state of the VAP-SIRS model is obtained by setting the derivatives of the ODE system 1 to

0. A straightforward computation reduces the endemic system of equations to the following:

$$0 = (\beta I + \delta^{+} I_{V}) \left(d - I - \frac{\gamma}{\kappa} I \right) - \gamma I$$

$$0 = \frac{v_{1}^{*} \alpha \left(v_{2} + \beta I + \delta^{*} I_{V} \right) \cdot \gamma I_{V}}{(\beta I + \delta^{*} I_{V} + v_{2} + v_{1}^{*} \left(1 - \alpha \right))}$$

$$-v_{2} \left(1 - d - I_{V} - \frac{\gamma}{\kappa + v_{1}^{*}} I_{V} \right) (\beta I + \delta^{*} I_{V})$$

$$+v_{2} \gamma I_{V} + v_{1}^{*} \frac{\gamma}{\kappa + v_{1}^{*}} I_{V} \cdot (\beta I + \delta^{*} I_{V})$$

$$S = d - I \left(1 + \frac{\gamma}{\kappa} \right)$$

$$S_{V} = \frac{\gamma I_{V}}{\beta I + \delta^{*} I_{V}}$$

$$R = \frac{\gamma}{\kappa} I$$

$$R_{V} = \frac{\gamma}{\kappa + v_{1}} I_{V}$$

$$V = 1 - d - S - Sv - I - Iv - R - Rv,$$

$$(9)$$

where for the proportional mixing we have: $\delta^* = \delta$ and $\delta^+ = \beta$, and for the preferential mixing we set $\delta^* = \frac{\delta^2}{\beta d + \delta(1-d)}$ and $\delta^+ = \frac{\beta^2}{\beta d + \delta(1-d)}$. The roots of the Equations 9 and 10 are plotted in Figures 4 and 5.

Data and materials availability The VAP-SIRS model was implemented using R version 4.0.2 along
with the shiny package to build an interactive web application that allows to simulate the model. The
code of the model is available online in the GitHub repository: https://github.com/storaged/
VAP-SIRS, and the on-line tool is available http://bioputer.mimuw.edu.pl:85/VAP-SIRS/.
The code to generate Figures 2-5 from the main text is available at https://github.com/eMaerthin/
VAP_SIRS_Ananysis.

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- Authors contributions AG, KG, TK, and ES conceived the VAP-SIRS model with input and feed-
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- implemented model simulations and the Shiny application for visualizations. MB implemented the sta-
- bility analysis. SC, TC, EP, and MR performed literature search. ES supervised the study. All authors
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